

## PRACTICE 01 – MEASUREMENTS ON COAXIAL CABLES



### 1. CALIBRATION OF THE NETWORK ANALYSER (VNA)

**Calibrate FULL 2 PORT** for 3 times (one for each component of the group). Frequency range:  $f_{min} \div 1\text{GHz}$ ;  $f_{min} \div 2\text{ GHz}$ ;  $f_{min} \div 3\text{ GHz}$ . ( $f_{min}$  depends on the particular VNA).

Follow the instructions in the calibration sheet to acquire, save and plot data. **(REPORT)**

### 2. TRANSMISSION MEASUREMENTS ON COAXIAL CABLE

On the desk, there is a coaxial cable with type-N connectors being **L** its **physical length** (different for each desk). Connect the cable to the 2 ports of the VNA calibrated between  $f_{min}$  and 3 GHz.

Theoretical  $S_{21}$  of the cable is:

$$S_{21}(\omega) = \exp(-\gamma L) = \exp(-\alpha L - j\beta L) = \exp(-\alpha' \sqrt{\omega} L - j \omega \tau)$$

Evaluate the attenuation constant  $\alpha$  at 1 GHz **(REPORT)**.

### 3. S21 PHASE MEASUREMENT

Select Format-Phase. Why do you see a periodic signal between  $-180^\circ$  and  $180^\circ$ ? **(REPORT)**.

The commands

(VNA1 and VNA2) -> RESPONSE-> **SCALE-> Electrical Delay**

(PNA) -> **SCALE -> Electrical Delay**

(FIELD FOX) -> **SCALE/AMPLITUDE ->more => Electrical Delay**

add a (fictious) delay to the signal, thus you are measuring

$$S21' = S21 \exp(j\omega\tau').$$

Therefore, the phase of the measured  $S21'$  becomes

$$\text{phase}(S21') = -\omega\tau + \omega\tau'.$$

When  $-\omega\tau + \omega\tau' = 0$ , the phase plot shall become a horizontal line.

The VNA shows the value of  $\tau'$  (electrical delay) in seconds and the cable length  $L0 = c \tau'$  (**electrical length of the cable**, with  $c$  speed of light in vacuum/air), i.e. assuming a line in vacuum. **(REPORT)**.

On the contrary, in the cable there is a dielectric material with constant  $\epsilon_r$ , thus the EM field has a phase velocity  $v=c/\sqrt{\epsilon_r}$  and length  $L=c\tau'/\sqrt{\epsilon_r}$ .

Thus  $L0/L = \sqrt{\epsilon_r} = n$  (refractive index of the dielectric material)

Measuring  $L$  with a meter, evaluate the **permittivity**  $\epsilon_r$  and the **refractive index**  $n$  for the cable under test **(REPORT)**.

#### 4. S21 MAGNITUDE MEASUREMENT (dB)

Select Format-Log mag. Measure **S21(f)** which is decreasing as frequency  $f$  increases **(REPORT)**.

As we know from theory

$$\text{mod}(S_{21})\text{dB} = 20\log_{10}(\exp[-\alpha' \sqrt{\omega}L]) =$$

$$-20 (\log_{10}e) \alpha' \sqrt{2\pi} \sqrt{f} L = -8,686 \alpha' \sqrt{2\pi} L \sqrt{f}.$$

Execute the regression (**LinearFit**), with the  $\sqrt{f}$  on the x-axis, derive the slope and thus the **constant  $\alpha'$  with its uncertainty**. Use  $\alpha'$  to give also the **attenuation of the cable** at 1 GHz in dB/m with its uncertainty **(REPORT)**.

#### 5. CABLE REFLECTION MEASUREMENTS

Connect the coaxial cable to VNA port 1, leaving open the other end.

Plot the magnitude of S11 in dB, being  $\Delta f$  the period of  $|S_{11}|$  oscillations. **(REPORT)**.

Use  $\Delta f$  to measure **the delay  $\tau$**  of the cable ( $\tau = 1/(2\Delta f)$ ) and compare it with the one you evaluated previously **(REPORT)**.

Evaluate the **refractive index  $n$**  using the formula:

$$n = c / (2 L \Delta f)$$

and compare it with the previous result **(REPORT)**.